

04. Pseudocode Solved PYQs & Comprehensive Practice Bank

Module Focus: 20 Questions in 20 Minutes

Key Skills: Bitwise Operator Tracing, Loop Execution Limits, Pass-by-Reference/Value, Recursion Call Stack Unwinding, Array Bit Manipulation, Operator Precedence

1. Bitwise Operations PYQ Bank

PYQ 1: Bitwise XOR and AND Combination

```
Integer a, b, c
Set a = 5, b = 10, c = 2
If ((a ^ b ^ c) > (a & b & c))
    a = b ^ c
    b = a + c
Else
    c = a & b
    a = b + c
End If
Print a + b + c
```

Step-by-Step Execution Trace:

- Binary Representation:** - $a = 5 = 0101_2$ - $b = 10 = 1010_2$ - $c = 2 = 0010_2$
- Evaluate Condition $(a \oplus b \oplus c) > (a \& b \& c)$:** - $a \oplus b = 0101_2 \oplus 1010_2 = 1111_2 = 15$. - $15 \oplus c = 1111_2 \oplus 0010_2 = 1101_2 = 13$. Left side $= 13$. - $a \& b = 0101_2 \& 1010_2 = 0000_2 = 0$. - $0 \& c = 0$. Right side $= 0$. - Condition $13 > 0$ is **TRUE!**
- Execute THEN block:** - $a = b \oplus c$ $\implies 10 \oplus 2 = 1010_2 \oplus 0010_2 = 1000_2 = 8$. (Now $a = 8$). - $b = a + c$ $\implies 8 + 2 = 10$. (Now $b = 10$).
- Compute Final Expression $a + b + c$:** - $a = 8$, $b = 10$, $c = 2$. - $8 + 10 + 2 = 20$.

Final Output: 20

PYQ 2: Bit Shift Arithmetic Combined with Logical Negation

```
Integer p = 12, q = 3, r = 0
r = (p >> 2) + (q << 2)
If ((r & 1) == 0)
    p = r ^ q
Else
    q = r & p
```

```
End If
Print p + q + r
```

Step-by-Step Execution Trace:

- Bit Shifts:** - $p \gg 2$ $\implies 12 \gg 2 = \lfloor 12 / 2^2 \rfloor = \lfloor 12 / 4 \rfloor = 3$. - $q \ll 2$ $\implies 3 \ll 2 = 3 \times 2^2 = 3 \times 4 = 12$. - $r = 3 + 12 = 15$.
- Condition Check** $(r \& 1) == 0$: - $15 \& 1 = 1111_2 \& 0001_2 = 1$. - $(1 == 0)$ evaluates to **FALSE**.
- Execute ELSE block:** - $q = r \& p$ $\implies 15 \& 12 = 1111_2 \& 1100_2 = 1100_2 = 12$. (Now $q = 12$).
- Compute Final Sum** $p + q + r$: - $p = 12, q = 12, r = 15$. - $12 + 12 + 15 = 39$.

Final Output: 39

PYQ 3: Complex Nested Bitwise & Subtraction Loop

```
Integer a = 14, b = 7, c = 0
While (a > b)
    c = c + (a & b)
    a = a - 2
    b = b + 1
End While
Print c
```

Step-by-Step Execution Trace Table:

Iteration	Initial a	Initial b	Condition (a > b)	a & b Calculation	Updated c	Updated a	Updated b
Start	14	7	-	-	0	14	7
Pass 1	14	7	$14 > 7$ (True)	$1110_2 \& 0111_2 = 0110_2 = 6$	$0 + 6 = 6$	$14 - 2 = 12$	$7 + 1 = 8$
Pass 2	12	8	$12 > 8$ (True)	$1100_2 \& 1000_2 = 1000_2 = 8$	$6 + 8 = 14$	$12 - 2 = 10$	$8 + 1 = 9$
Pass 3	10	9	$10 > 9$ (True)	$1010_2 \& 1001_2 = 1000_2 = 8$	$14 + 8 = 22$	$10 - 2 = 8$	$9 + 1 = 10$
Pass 4	8	10	$8 > 10$ (FALSE)	Loop Terminates	22	8	10

Final Output: 22

PYQ 4: Bitwise OR, XOR, AND with Shift Operators

```
Integer a = 8, b = 5, c = 3
c = (a >> 1) ^ (b << 1)
If ((c | a) > (c & b))
    a = (a ^ b) + c
```

```

    b = b & c
Else
    c = c ^ a
End If
Print a + b + c

```

Step-by-Step Execution Trace:

- 1. Bit Shift and Initial XOR Assignment:** - $a \gg 1$ $\implies 8 \gg 1 = 4 = 0100_2$. - $b \ll 1$ $\implies 5 \ll 1 = 10 = 1010_2$. - $c = 4 \wedge 10$ $\implies 0100_2 \oplus 1010_2 = 1110_2 = 14$.
- 2. Evaluate Condition $(c \mid a) > (c \& b)$:** - $c \mid a$ $\implies 14 \mid 8 = 1110_2 \mid 1000_2 = 1110_2 = 14$. - $c \& b$ $\implies 14 \& 5 = 1110_2 \& 0101_2 = 0100_2 = 4$. - Condition $14 > 4$ is **TRUE**.
- 3. Execute THEN block:** - $a = (a \wedge b) + c$ $\implies (8 \oplus 5) + 14 = (1000_2 \oplus 0101_2) + 14 = 13 + 14 = 27$. (Now $a = 27$). - $b = b \& c$ $\implies 5 \& 14 = 0101_2 \& 1110_2 = 0100_2 = 4$. (Now $b = 4$).
- 4. Compute Final Expression $a + b + c$:** - $a = 27, b = 4, c = 14$. - $27 + 4 + 14 = 45$.

Final Output: 45

PYQ 5: Bitwise Accumulation Loop with AND & OR

```

Integer a = 7, b = 11, c = 0
For (Integer i = 1 to 3)
    c = c + ((a & i) ^ (b \ i))
End For
Print c

```

Step-by-Step Execution Trace Table:

Iteration i	$a \& i$ Binary & Value	$b \setminus i$ Binary & Value	$(a \& i) \wedge (b \setminus i)$ Calculation	Updated c
Start	-	-	-	0
$i = 1$	$0111_2 \& 0001_2 = 1$	$1011_2 \setminus 0001_2 = 1011_2 = 11$	$0001_2 \oplus 1011_2 = 1010_2 = 10$	$0 + 10 = 10$
$i = 2$	$0111_2 \& 0010_2 = 2$	$1011_2 \setminus 0010_2 = 1011_2 = 11$	$0010_2 \oplus 1011_2 = 1001_2 = 9$	$10 + 9 = 19$
$i = 3$	$0111_2 \& 0011_2 = 3$	$1011_2 \setminus 0011_2 = 1011_2 = 11$	$0011_2 \oplus 1011_2 = 1000_2 = 8$	$19 + 8 = 27$

Final Output: 27

2. Recursion & Stack Unwinding PYQ Bank

PYQ 6: Double Recursive Call Tree Tracing

```
Integer fun(Integer n)
    If (n <= 0)
        Return 0
    End If
    If (n == 1)
        Return 2
    End If
    Return fun(n - 1) + fun(n - 2) + n
End Function
```

What is the return value of fun(4)?

Step-by-Step Stack Unwinding Trace: 1. Base Cases: - $\text{fun}(0) = 0$ - $\text{fun}(1) = 2$ 2. Evaluate $\text{fun}(2)$: - $\text{fun}(2) = \text{fun}(1) + \text{fun}(0) + 2 = 2 + 0 + 2 = 4$. 3. Evaluate $\text{fun}(3)$: - $\text{fun}(3) = \text{fun}(2) + \text{fun}(1) + 3 = 4 + 2 + 3 = 9$. 4. Evaluate $\text{fun}(4)$: - $\text{fun}(4) = \text{fun}(3) + \text{fun}(2) + 4 = 9 + 4 + 4 = 17$.

Final Output: 17

PYQ 7: Recursive Function with Static Variable State

```
Integer fun(Integer n)
    Static Integer count = 0
    If (n <= 0)
        Return count
    End If
    count = count + n
    Return fun(n - 1) + fun(n - 2)
End Function
```

What is the value returned by fun(3)?

Step-by-Step Call Order & State Unwinding: 1. $\text{fun}(3)$: `count` updated $\$ \implies 0 + 3 = 3\$$. Calls $\text{fun}(2)$ + $\text{fun}(1)$. 2. Left Child $\text{fun}(2)$ executes first: - `count` updated $\$ \implies 3 + 2 = 5\$$. Calls $\text{fun}(1)$ + $\text{fun}(0)$. - Left Child $\text{fun}(1)$ executes: - `count` updated $\$ \implies 5 + 1 = 6\$$. Calls $\text{fun}(0)$ + $\text{fun}(-1)$. - $\text{fun}(0)$ returns current `count` $\$ = 6\$$. - $\text{fun}(-1)$ returns current `count` $\$ = 6\$$. - $\text{fun}(1)$ unwinds $\$ \implies 6 + 6 = 12\$$. - Right Child $\text{fun}(0)$ of $\text{fun}(2)$ executes: - Returns current `count` $\$ = 6\$$. - $\text{fun}(2)$ unwinds $\$ \implies 12 + 6 = 18\$$. 3. Right Child $\text{fun}(1)$ of $\text{fun}(3)$ executes: - `count` updated $\$ \implies 6 + 1 = 7\$$. Calls $\text{fun}(0)$ + $\text{fun}(-1)$. - $\text{fun}(0)$ returns current `count` $\$ = 7\$$. - $\text{fun}(-1)$ returns current `count` $\$ = 7\$$. - $\text{fun}(1)$ unwinds $\$ \implies 7 + 7 = 14\$$. 4. Root $\text{fun}(3)$ unwinds: - $\text{fun}(3) = \text{fun}(2) + \text{fun}(1) = 18 + 14 = 32$.

Final Output: 32

PYQ 8: Recursive Function with Bitwise XOR & Unwinding Step

```
Integer foo(Integer a, Integer b)
    If (b <= 0)
        Return a
    End If
    Return foo(a ^ b, b - 1) + b
End Function
What is the output of foo(5, 3)?
```

Step-by-Step Call Stack Recursion Trace: - **Call 1:** `foo(5, 3)` - $b = 3 > 0$. Bitwise XOR: $a \oplus b = 5 \oplus 3 = 0101_2 \oplus 0011_2 = 0110_2 = 6$. - Returns `foo(6, 2) + 3`. - **Call 2:** `foo(6, 2)` - $b = 2 > 0$. Bitwise XOR: $a \oplus b = 6 \oplus 2 = 0110_2 \oplus 0010_2 = 0100_2 = 4$. - Returns `foo(4, 1) + 2`. - **Call 3:** `foo(4, 1)` - $b = 1 > 0$. Bitwise XOR: $a \oplus b = 4 \oplus 1 = 0100_2 \oplus 0001_2 = 0101_2 = 5$. - Returns `foo(5, 0) + 1`. - **Call 4:** `foo(5, 0)` - $b = 0 \leq 0$. **Base Case Reached!** Returns $a = 5$.

Stack Unwinding: - `foo(5, 0) = 5` - `foo(4, 1) = 5 + 1 = 6` - `foo(6, 2) = 6 + 2 = 8` - `foo(5, 3) = 8 + 3 = 11`

Final Output: `11`

PYQ 9: Alternating Parity Recursive Function

```
Integer solve(Integer n, Integer k)
    If (n <= 1)
        Return k
    End If
    If (n Mod 2 == 0)
        Return solve(n / 2, k + n)
    Else
        Return solve(n - 1, k * 2)
    End If
End Function
What is the return value of solve(6, 2)?
```

Step-by-Step Tail-Recursive Execution: 1. `solve(6, 2)` : $n=6$ (Even) $\implies$ Returns `solve(6 / 2, 2 + 6)` $=$ `solve(3, 8)`. 2. `solve(3, 8)` : $n=3$ (Odd) $\implies$ Returns `solve(3 - 1, 8 * 2)` $=$ `solve(2, 16)`. 3. `solve(2, 16)` : $n=2$ (Even) $\implies$ Returns `solve(2 / 2, 16 + 2)` $=$ `solve(1, 18)`. 4. `solve(1, 18)` : $n=1 \leq 1$ (Base Case) $\implies$ Returns $k = 18$.

Final Output: `18`

3. Loop Execution & State Table PYQ Bank

PYQ 10: REPEAT-UNTIL Off-by-One Counter Verification

```
Integer i = 1, sum = 0
REPEAT
    sum = sum + i * i
    i = i + 1
UNTIL (i > 4)
Print sum
```

Step-by-Step Execution Trace: - **Pass 1:** `sum = 0 + (1 * 1) = 1`, `i = 2`. Condition `(2 > 4)` is **FALSE** \$ \to\$ Continue. - **Pass 2:** `sum = 1 + (2 * 2) = 5`, `i = 3`. Condition `(3 > 4)` is **FALSE** \$ \to\$ Continue. - **Pass 3:** `sum = 5 + (3 * 3) = 14`, `i = 4`. Condition `(4 > 4)` is **FALSE** \$ \to\$ Continue. - **Pass 4:** `sum = 14 + (4 * 4) = 30`, `i = 5`. Condition `(5 > 4)` is **TRUE** \$ \to\$ **TERMINATE!**

Final Output: `30` (Computes sum of squares $1^2 + 2^2 + 3^2 + 4^2 = 1 + 4 + 9 + 16 = 30$).

PYQ 11: Nested For Loops with Conditional Bitwise Accumulation

```
Integer sum = 0
For (Integer i = 1 to 3)
    For (Integer j = i to 3)
        If ((i + j) Mod 2 == 0)
            sum = sum + (i ^ j)
        Else
            sum = sum + (i & j)
        End If
    End For
End For
Print sum
```

Step-by-Step Execution Trace Table:

Outer i	Inner j	i + j	Parity	Evaluated Operation	Operation Result	Updated sum
1	1	2	Even	$1 \oplus 1 = 0001_2 \oplus 0001_2$	0	$0 + 0 = 0$
1	2	3	Odd	$1 \& 2 = 0001_2 \& 0010_2$	0	$0 + 0 = 0$
1	3	4	Even	$1 \oplus 3 = 0001_2 \oplus 0011_2$	2	$0 + 2 = 2$
2	2	4	Even		0	$2 + 0 = 2$

Outer <code>i</code>	Inner <code>j</code>	<code>i + j</code>	Parity	Evaluated Operation	Operation Result	Updated <code>sum</code>
				$2 \oplus 2 = 0010_2 \oplus 0010_2$		
2	3	5	Odd	$2 \& 3 = 0010_2 \& 0011_2$	2	$\$2 + 2 = 4\$$
3	3	6	Even	$3 \oplus 3 = 0011_2 \oplus 0011_2$	0	$\$4 + 0 = 4\$$

Final Output: `4`

PYQ 12: Digit Extraction Loop with Parity Branching

```

Integer n = 456, sum = 0, rem = 0
While (n > 0)
    rem = n Mod 10
    If (rem Mod 2 != 0)
        sum = sum + rem * 2
    Else
        sum = sum + rem
    End If
    n = n / 10
End While
Print sum

```

Step-by-Step Execution Trace Table:

Iteration	Initial <code>n</code>	<code>rem = n Mod 10</code>	<code>rem Mod 2 != 0</code>	Applied Operation	Updated <code>sum</code>	<code>n = n / 10</code>
Pass 1	456	6	False (Even)	<code>sum + rem</code>	$\$0 + 6 = 6\$$	45
Pass 2	45	5	True (Odd)	<code>sum + rem * 2</code>	$\$6 + (5 \times 2) = 16\$$	4
Pass 3	4	4	False (Even)	<code>sum + rem</code>	$\$16 + 4 = 20\$$	0
Pass 4	0	-	$0 > 0$ False	Loop Terminates	20	0

Final Output: `20`

PYQ 13: Bitwise Right Shift & XOR Accumulator Loop

```

Integer x = 15, y = 9, z = 0
While (x > 0)
    z = z + (x & 1)

```

```

x = x >> 1
y = y ^ x
End While
Print z, y

```

Step-by-Step Execution Trace Table:

Iteration	Initial x	x & 1	Updated z	x >> 1 (New x)	y ^ x Calculation	Updated y
Start	15 (\$1111_2\$)	-	0	-	-	9 (\$1001_2\$)
Pass 1	15	1	\$0 + 1 = 1\$	7 (\$0111_2\$)	\$9 \oplus 7 = 1001_2 \oplus 0111_2 = 1110_2\$	14
Pass 2	7	1	\$1 + 1 = 2\$	3 (\$0011_2\$)	\$14 \oplus 3 = 1110_2 \oplus 0011_2 = 1101_2\$	13
Pass 3	3	1	\$2 + 1 = 3\$	1 (\$0001_2\$)	\$13 \oplus 1 = 1101_2 \oplus 0001_2 = 1100_2\$	12
Pass 4	1	1	\$3 + 1 = 4\$	0 (\$0000_2\$)	\$12 \oplus 0 = 1100_2 \oplus 0000_2 = 1100_2\$	12
Pass 5	0	-	Loop Ends	0	-	12

Final Output: **4 12**

4. Pass-by-Reference & Array Tracing PYQ Bank

PYQ 14: Pass-by-Reference Modifying Outer Variables

```

Function modify(Integer &x, Integer y)
    x = x * 2
    y = y + 5
    Return x + y
End Function

Main:
    Integer a = 5, b = 10, res
    res = modify(a, b)
    Print a, b, res
End Main

```

Step-by-Step Execution Trace: 1. **a** is passed **by reference** (**&x**), so changes to **x** directly mutate variable **a**. 2. **b** is passed **by value** (**y**), so **y** is a local copy; variable **b** remains unaffected. 3. Inside **modify**: - **x = x * 2** \$\implies x = 5 \times 2 = 10\$. Variable **a** becomes **10**. - **y = y + 5** \$\implies y = 10 + 5 = 15\$. Variable **b** stays **10**. - Returns **10 + 15 = 25**. 4. Printing **a, b, res**: - **a = 10**, **b = 10**, **res = 25**.

Final Output: 10 10 25

PYQ 15: Pass-by-Reference Bitwise Swap and Sum

```
Function update(Integer &a, Integer b, Integer &c)
    a = a ^ b
    b = b ^ a
    c = a + b
    Return a * b
End Function

Main:
    Integer x = 6, y = 4, z = 2, ans
    ans = update(x, y, z)
    Print x, y, z, ans
End Main
```

Step-by-Step Parameter Mutation Trace: 1. `x` is passed by reference (`&a`) $\implies$ modifications to `a` directly alter outer `x`. 2. `y` is passed by value (`b`) $\implies$ modifications to `b` do NOT affect outer `y`. 3. `z` is passed by reference (`&c`) $\implies$ modifications to `c` directly alter outer `z`. 4. Inside `update` : - `a = a ^ b` $\implies 6 \oplus 4 = 0110_2 \oplus 0100_2 = 0010_2 = 2$. (Outer `x` becomes `2`). - `b = b ^ a` $\implies 4 \oplus 2 = 0100_2 \oplus 0010_2 = 0110_2 = 6$. (Local `b` $\$=$ 6; outer `y` stays `4`). - `c = a + b` $\implies 2 + 6 = 8$. (Outer `z` becomes `8`). - `Return a * b` $\implies 2 \times 6 = 12$. 5. In `Main` : - `x = 2` , `y = 4` , `z = 8` , `ans = 12` .

Final Output: 2 4 8 12

PYQ 16: Array Traversal with Bit Shift & Conditional Accumulation

```
Integer A[5] = {4, 7, 12, 15, 8}
Integer total = 0
For (Integer i = 0 to 4)
    If ((A[i] & 1) == 0)
        total = total + (A[i] >> 1)
    Else
        total = total + (A[i] << 1)
    End If
End For
Print total
```

Step-by-Step Execution Trace Table:

Index <code>i</code>	Array Element <code>A[i]</code>	<code>A[i] & 1</code> Check	Parity Branch	Shift Operation & Value	Updated <code>total</code>
0	4	$4 \& 1 = 0$			$0 + 2 = 2$

Index <code>i</code>	Array Element <code>A[i]</code>	<code>A[i] & 1</code> Check	Parity Branch	Shift Operation & Value	Updated <code>total</code>
			Even (<code>== 0</code>)	$4 \gg 1 = \lfloor 4/2 \rfloor = 2$	
1	7	$7 \& 1 = 1$	Odd (<code>!= 0</code>)	$7 \ll 1 = 7 \times 2 = 14$	$2 + 14 = 16$
2	12	$12 \& 1 = 0$	Even (<code>== 0</code>)	$12 \gg 1 = \lfloor 12/2 \rfloor = 6$	$16 + 6 = 22$
3	15	$15 \& 1 = 1$	Odd (<code>!= 0</code>)	$15 \ll 1 = 15 \times 2 = 30$	$22 + 30 = 52$
4	8	$8 \& 1 = 0$	Even (<code>== 0</code>)	$8 \gg 1 = \lfloor 8/2 \rfloor = 4$	$52 + 4 = 56$

Final Output: `56`

5. Operator Precedence & Conditional Logic Bank

PYQ 17: Bitwise AND vs XOR Operator Precedence Tracing

```
Integer p = 5, q = 3, r = 8
Integer res = (p + q * 2) ^ (r >> 2) & 7
Print res
```

Step-by-Step Precedence & Binary Evaluation:

- 1. Parentheses & Arithmetic:** - `(p + q * 2)` $\implies 5 + (3 \times 2) = 5 + 6 = 11 = 1011_2$. - `(r >> 2)` $\implies 8 \gg 2 = 2 = 0010_2$. - Expression reduces to: `11 ^ 2 & 7`.
- 2. Bitwise Operator Precedence (`&` higher than `^`):** - Evaluate `2 & 7` first: $0010_2 \& 0111_2 = 0010_2 = 2$.
- 3. Evaluate Bitwise XOR (`^`):** - `11 ^ 2` $\implies 1011_2 \oplus 0010_2 = 1001_2 = 9$.

Final Output: `9`

PYQ 18: Ternary Operator Evaluation with Relational Precedence

```
Integer x = 10, y = 20, z = 15, ans
ans = (x ^ y > z) ? ((y >> 2) + x) : ((x << 1) ^ z)
Print ans
```

Step-by-Step Precedence & Execution:

- 1. Evaluate Condition `(x ^ y > z)`:** - Relational operator `>` has higher precedence than bitwise `^`. - `y > z` $\implies 20 > 15 \implies 1$ (True). - Expression becomes `x ^ 1` $\implies 10 \oplus 1 = 1010_2 \oplus 0001_2 = 1011_2 = 11$. - Non-zero integer `11` evaluates to **TRUE** in C.

boolean condition context. 2. **Execute TRUE Expression** $((y >> 2) + x)$: - $y >> 2$ $\implies 20 \gg 2 = 5$.
 - $5 + x$ $\implies 5 + 10 = 15$. 3. **Assign & Print**: - $ans = 15$.

Final Output: 15

6. Web-Researched CoCubes, Sanfoundry & GFG High-Frequency PYQ Expansion

PYQ 19: CoCubes Bitwise XOR Inequality Branching Trap

```
Integer a = 6, b = 8, c = 15
If ((b ^ a) < a)
    b = a
End If
Print a + b + c
```

Step-by-Step Binary Execution Trace: 1. **Binary Conversions:** - $a = 6 = 0110_2$ - $b = 8 = 1000_2$ - $c = 15 = 1111_2$ 2. **Evaluate Condition** $(b \wedge a) < a$: - $b \oplus a = 1000_2 \oplus 0110_2 = 1110_2 = 14$. - Evaluate $14 < 6$ $\implies$ **FALSE**. 3. **Branch Decision:** - The **If** condition fails, so $b = a$ is **skipped**. b remains **8**. 4. **Compute Final Output** $a + b + c$: - $6 + 8 + 15 = 29$.

State Table Summary: | Operation | Left Side | Right Side | Condition | Action Taken | Final Value | | :---: | :---: | :---: | :---: | | $b \wedge a$ | $1000_2 \oplus 0110_2 = 14$ | $a = 6$ | $14 < 6$ (FALSE) | Skip $b = a$ | $b = 8$ | | $a + b + c$ | $6 + 8 + 15$ | - | - | Print Output | **29** |

Final Output: 29

PYQ 20: CoCubes Recursive Parameter Swapper & Accumulator

```
Function solve(Integer a, Integer b)
    If (a < b)
        Return solve(b, a)
    Else If (b != 0)
        Return (a + solve(a, b - 1))
    Else
        Return 0
    End If
End Function
```

What is the returned value of $\text{solve}(8, 9)$?

Step-by-Step Recursive Call Stack Unwinding Table: 1. **Call 1:** $\text{solve}(8, 9)$ $\implies (8 < 9)$ is **TRUE**. Returns $\text{solve}(9, 8)$ (Parameter order swapped so $a \geq b$). 2. **Call 2 to Call 10 Winding Phase:** $\text{solve}(9, 8)$ calls $9 + \text{solve}(9, 7)$ down to $\text{solve}(9, 0)$.

Call Level	Invocation	Condition / Action	Returned Value / Expression	Accumulated Value
Level 10	<code>solve(9, 0)</code>	Base Case <code>b == 0</code>	Returns <code>0</code>	0
Level 9	<code>solve(9, 1)</code>	<code>9 + solve(9, 0)</code>	<code>\$9 + 0\$</code>	9
Level 8	<code>solve(9, 2)</code>	<code>9 + solve(9, 1)</code>	<code>\$9 + 9\$</code>	18
Level 7	<code>solve(9, 3)</code>	<code>9 + solve(9, 2)</code>	<code>\$9 + 18\$</code>	27
Level 6	<code>solve(9, 4)</code>	<code>9 + solve(9, 3)</code>	<code>\$9 + 27\$</code>	36
Level 5	<code>solve(9, 5)</code>	<code>9 + solve(9, 4)</code>	<code>\$9 + 36\$</code>	45
Level 4	<code>solve(9, 6)</code>	<code>9 + solve(9, 5)</code>	<code>\$9 + 45\$</code>	54
Level 3	<code>solve(9, 7)</code>	<code>9 + solve(9, 6)</code>	<code>\$9 + 54\$</code>	63
Level 2	<code>solve(9, 8)</code>	<code>9 + solve(9, 7)</code>	<code>\$9 + 63\$</code>	72
Level 1	<code>solve(8, 9)</code>	Returns <code>solve(9, 8)</code>	Returns Level 2 result	72

Final Output: **72**

PYQ 21: CoCubes Decrement Modification Loop Trap

```
Integer n
For (n = 3; n != 0; n--)
    Print n
    n = n - 1
End For
```

Step-by-Step State Table Trace: | Iteration | Initial `n` | Condition `n != 0` | Body Action (`Print n`) | Internal Mutation (`n = n - 1`) | Post Loop Decrement (`n--`) | Value for Next Test | | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

| :---: | | **1** | **3** | `3 != 0 (TRUE)` | Prints `3` | `n = 3 - 1 = 2` | `n = 2 - 1 = 1` | **1** | | **2** | **1** | `1 != 0 (TRUE)` | Prints `1` | `n = 1 - 1 = 0` | `n = 0 - 1 = -1` | **-1** | | **3** | **-1** | `-1 != 0 (TRUE)` | Prints `-1` | `n = -1 - 1 = -2` | `n = -2 - 1 = -3` | **-3** | | **4** | **-3** | `-3 != 0 (TRUE)` | Prints `-3` | `n = -3 - 1 = -4` | `n = -4 - 1 = -5` | **-5** |

- **Key Observation:** Notice how `n` skips `0` completely! It transitions from `1` to `0` inside body `$\to$` `-1` after loop header `n--`.
- **Termination Check:** `n != 0` will remain **TRUE** for all negative odd integers.

Final Output: Infinite Loop

PYQ 22: Sanfoundry REPEAT-UNTIL Shift & Mask Counter

```
Integer p = 10, q = 3, count = 0
REPEAT
```

```

count = count + 1
p = p >> 1
q = q + (p & 1)
UNTIL (p <= 1)
Print count, p, q

```

Step-by-Step Variable State Table: | Pass | Initial | `p` | `count = count + 1` | `p = p >> 1` | `p & 1` | `q = q + (p & 1)` | UNTIL Test (`p <= 1`) | Evaluation | | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | | **Start** | 10 | 0 | - | - | 3 | - | - | | **Pass 1** | 10 | **1** | $10 \bmod 2 = 0$ (`0101`) | $10 \gg 1 = 5$ (`0010`) | $1 \& 1 = 1$ (`0001`) | $3 + 1 = 4$ (`0100`) | **FALSE** | Continue | | **Pass 2** | 5 | **2** | $5 \bmod 2 = 1$ (`0010`) | $5 \gg 1 = 2$ (`0010`) | $2 \& 1 = 0$ (`0000`) | $4 + 0 = 4$ (`0100`) | **FALSE** | Continue | | **Pass 3** | 2 | **3** | $2 \bmod 2 = 0$ (`0001`) | $2 \gg 1 = 1$ (`0001`) | $3 \& 1 = 1$ (`0001`) | $4 + 1 = 5$ (`0101`) | **TRUE** | **TERMINATE** |

• **Final Values:** `count = 3`, `p = 1`, `q = 5`.

Final Output: `3 1 5`

PYQ 23: GFG Bitwise Left Shift with Two's Complement NOT Operator

```

Integer a = 7, b = 2, c = 0
c = ((~a) << b) + (a ^ b)
Print c

```

Step-by-Step Binary State Table: | Step | Operation / Sub-expression | 8-Bit Binary Computation | Decimal Result | Notes | | :---: | :---: | :---: | :---: | :---: | | **1** | `a` | `0000 0111` | **7** | Input Value | | **2** | `~a` | `1111 1000` | **-8** | Bitwise NOT identity $\sim a = -(a + 1) = -8$ | | **3** | `(~a) << b` | `11111000_2 \gg 2 = 1110_2` | **-32** | Shift left by 2 ($(-8) \times 4 = -32$) | | **4** | `a ^ b` | `00000111_2 \oplus 0000010_2 = 0000_2` | **5** | Bitwise XOR of 7 and 2 | | **5** | `c = (-32) + 5` | $-32 + 5 = -27$ | Addition of components |

Final Output: `-27`



Quick Summary Checklist for Exam Mastery

- Bitwise Shifts:**
- Left Shift ($x \ll n$) $= x \times 2^n$
- Right Shift ($x \gg n$) $= \lfloor x / 2^n \rfloor$
- Bitwise Parity Check:**
- $(x \& 1) == 0$ implies x is **Even**
- $(x \& 1) == 1$ implies x is **Odd**
- Bitwise Identity Properties:**
- $x \oplus x = 0$
- $x \oplus 0 = x$
- $x \& x = x$
- $x \mid x = x$
- Pass-by-Reference:**

13. Parameter prefixed with `&` modifies original calling variable.
14. Value parameter makes local copy, leaving outer variable intact.